Abstract Title: Evaluating Mathematical Knowledge for Teaching Using TKAS

MSP Project Name: Learning Mathematics for Teaching-Teacher Knowledge Assessment System (LMT-TKAS)

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120 word summary:
The Teacher Knowledge Assessment System (TKAS) is an online system for administering the Learning Mathematics for Teaching (LMT) assessment questions. LMT assessments focus on the specialized forms of knowledge teachers’ use in providing their students opportunities to develop deep mathematical knowledge. This session will provide an overview of the LMT assessments with a focus on the link between teachers’ specialized knowledge, instruction, and student learning. The session will also provide a practical overview of the available LMT assessments and the feature available in online TKAS system for administering and analyzing LMT measures. We will also discuss how the TKAS system will be used to conduct a large-scale meta-analysis of MSPs and other professional development programs.

Section 1: Questions for dialogue at the MSP LNC.

What types of mathematical knowledge do teachers need in order to teach effectively? How is the knowledge used in effective mathematics teaching? How does this knowledge contribute to student learning? How do we ensure that all teachers have opportunities to develop this knowledge? This set of interrelated questions frame and define the research agenda of the Learning Mathematics for Teaching (LMT) project. Each of these questions has been a focus of inquiry across the projects research studies. To answer these questions it is critical to have a set of measures that can used to clearly specify and study teacher’s knowledge, its relation to valued outcomes such as student learning, and its development. In keeping with the theme of this year’s MSP LNC, we will highlight evidence that the LMT assessments identify features of teacher knowledge that are associated with student learning.

The session will also provide a practical overview of how the LMT assessments can provide tools for MSPs that will help them build links between the learning opportunities provided to teachers, teachers’ knowledge, and evidence gathered on student achievement. The focus will be on the Teacher Knowledge Assessment System (TKAS). TKAS is an online system for administering the Learning Mathematics for Teaching (LMT) assessment questions. The LMT questions are designed to measure mathematical knowledge for teaching in the areas of elementary and middle school geometry, patterns functions and algebra, number and operations, proportional reasoning, data statistics and probability, and rational number. For each of these areas there are parallel forms suitable for use as pre- and post-session assessments. Many MSP projects have successfully used the LMT measures to study teacher learning and assess program effects.

This session will demonstrate the capacity of TKAS. The system allows MSP users to create their own assessment plans by selecting content areas of interest and dates of administration. After teachers complete the assessment, MSP program leaders can download teacher data directly from TKAS and use the integrated analysis features to conduct a standard assessment analysis. The session will also cover
new TKAS features that are currently under development. These include online training and the
capacity for users to select questions and build their own tailored assessment form.

Finally, the session will discuss a research project that is being conducted using the TKAS
platform. All TKAS users are required to complete a survey reporting on the content and design of their
professional development program. This data will be used to conduct large-scale meta-analyses of the
effects of professional development on teacher learning.

Section 2: Conceptual framework.

Debates about what teachers need to know in order to teach and where they should learn that
knowledge stretch back to the 19th century (Hill, Ball, Sleep, & Lewis, 2007). Empirical studies soon
followed, and by the 1980s, there was accumulating evidence that teacher knowledge as measured by
tests of verbal facility or basic mathematical skills was a prime contributor to student achievement (e.g.,
Boardman, Davis & Sanday, 1977; Ferguson 1991; Hanushek 1972; Strauss & Sawyer, 1986). Over this
period there was also increasing public concern about the quality of the teacher corp. This led in the
1980s to the institution of basic-skills certification assessments for teachers, including those that
focused on basic mathematical knowledge. It has also led to a number of alternative certification
programs designed to increase the number of teachers with strong subject matter backgrounds, often at
the expense of having these recruits complete formal teacher education coursework (e.g., Teach for
America, American Board for Certification of Teacher Excellence).

Teacher educators object to the premise that strong subject matter training alone yields good
teaching, and have strenuously protested these new tests and certification routes (Darling-Hammond
and Youngs, 2002; Berliner, 2005). According to this view, measuring quality teachers through
performance in college or on tests of basic verbal or mathematics ability may overlook key elements in
what produces quality teaching. Chief among these elements, many propose, is profession-specific
knowledge of subject matter. Shulman (1986) and colleagues are widely seen as having sparked this line
of research by proposing the idea of “pedagogical content knowledge,” or knowledge that goes “beyond
knowledge of subject matter per se to the dimension of subject matter knowledge for teaching” (p. 9,
emphasis added). Components of pedagogical content knowledge, according to Shulman (1986), are
representations of specific content ideas, as well as an understanding of what makes the learning of a
specific topic difficult or easy for students.

The Learning Mathematics for Teaching (LMT) project’s work builds from Shulman’s observation
by focusing squarely on the question of the knowledge needed for teaching, and how that knowledge
can be developed in teachers. We have hypothesized a theoretical framework for defining and
organizing this knowledge and developed, pilot-tested, validated and disseminated a set of measures for
gauging teachers’ “mathematical knowledge for teaching” (MKT).

MKT includes all the mathematical knowledge used in carrying out the work of teaching, and
includes many of the elements described by Shulman, including pedagogical content knowledge (Ball,
Thames & Phelps, 2008). MKT differs from PCK, however, in that we more clearly articulate the
characteristics of the subject matter knowledge needed for teaching. In this view, teachers need
“common content knowledge,” or the mathematical knowledge that is used in common across many
professions. Knowing a number between 1.1 and 1.11, that zero is an even number, or how to multiply
35 x 25 are examples of this kind of knowledge. Another dimension of subject matter knowledge is
“specialized content knowledge”—or the mathematical knowledge and skill uniquely needed by
teachers in the conduct of their work. In looking for patterns in student errors or in sizing up whether a
non-standard approach works in general, teachers have to do a kind of mathematical work that others
do not. Many everyday tasks of teaching require mathematical knowledge of this kind, including
providing answers when students ask “why,” representing and linking representations of key mathematical ideas, and connecting new content to that already learned.

The Teacher Knowledge Assessment System provides an opportunity to test important hypotheses and questions about teacher knowledge and its development. The LMT assessments and associated surveys in TKAS provide a basis for studying professional development and teacher learning. When projects use TKAS to assess professional development, the PD provider and teachers involved in PD will complete surveys asking about the design of the professional development and about their own personal background. We will use this data along with both PD provider and teacher assessment scores to conduct a series of large-scale meta analyses to answer the following questions.

- What are the average effects for professional development programs on teachers’ mathematical knowledge for teaching?
- Do the effects of professional development programs vary by subject matter assessment and by program length? Do these effects vary by the average mathematics experience and pre-test knowledge of teacher participants?
- What features of professional development programs are consistently and most strongly associated with gains in teachers’ knowledge?
- Are particular program features more effective for teachers with different levels of mathematical knowledge, professional experience, and other teacher background characteristics?

Section 3: Explanatory framework

To ensure the integrity of these instruments, the LMT project has conducted in-depth psychometric and validation studies to determine how the instruments performed. We have conducted studies in the following areas.

- **Studies to identify constructs tapped by the measures.** We determined the dimensionality of our items by subjecting data from ten large-scale pilot forms (n=450-1000) to factor analyses and related analytic techniques (Reckase, 1985). Knowledge of content and students (KCS) items form a factor separate from subject matter knowledge, as hypothesized by our theoretical formulation. And we found that common and specialized content knowledge are distinguishable from one another (Hill, Schilling & Ball, 2004; Schilling, 2007). We also examined teacher and non-teacher reasoning and found that teachers use knowledge of content and students unique to the profession; non-teachers rarely used this knowledge (Hill, Dean & Goffney, 2007).

- **Studies to determine reliability of measures.** Each of the large-scale pilots is scaled and scored using Item Response Theory (IRT) methods and software. Reliabilities range from .50 for a specific set of KCS items to .90 with more recent forms. Technical reports for many of the forms are available at www.sitemaker.umich.edu/lmt under “summary of technical information.”

- **Studies to determine elemental validity.** Elemental validity determines whether specific items tap the knowledge they are designed to gauge, or whether they tap construct-irrelevant variance (e.g., reading ability, test-taking skills) (Schilling & Hill, 2007; Schilling, Blunk & Hill, 2007). We used cognitive interviews to investigate elemental validity, and found strong evidence for the validity of subject matter items.

- **Studies to determine ecological validity.** Ecological validity refers to the relationship of the test to its environment (Schilling & Hill, 2007). To determine ecological validity, we conducted two studies. In the first we predicted gains in student achievement using MKT and controlling for other critical background variables at the teacher, student, and school level (Hill, Rowan, & Ball,
We found a positive relationship between MKT and gains in student achievement in a sample of 125 schools and 600 teachers participating in school improvement programs. In the second study, we administered the multiple-choice measures and collected a sample (n=9) of lessons from ten teachers. Using a video coding rubric specifically designed to capture the mathematical quality of classroom work (e.g., presence of teacher errors; richness of the mathematics; teacher skill in understanding and using student ideas), we coded these lessons and found correlations of .5-.8 between facets of classroom mathematical quality and multiple-choice scores (Hill, Lusk, Charalambous, Lewis, Phelps, Sleep, & Ball, 2008).

- We have used these measures to evaluate the efficacy of a program intended to improve teachers’ mathematical knowledge. We found that the program did contribute to detectable teacher gains between pre- and post-test scores (Hill & Ball, 2004; Hill, Ball & Schilling, 2008). Our current research using the TKAS system is designed to expand this work and provide both more nuanced and robust analyses of professional development programs.
- External studies are also demonstrating the ecological validity of the measures. Of particular relevance in this year’s MSP LNC theme of establishing links to student achievement are recent studies that examine the relationships of teacher quality measures (including measures of knowledge) and student growth. The LMT measures have shown the strongest predictive relationships in such studies suggesting that they are powerful tool in assessing facets of teacher quality (Rockoff, et al., 2008).

In her 2004 AERA presidential address, Hilda Borko called for more rigorous study of teacher professional development. While acknowledging the importance of close qualitative work, Borko pointed to a pressing need for studies designed to examine the contributions of professional development across multiple contexts and for programs with different design features. She noted that these studies “will require new data collection and analysis tools—for example, instruments to measure change over time in teachers’ subject matter knowledge for teaching” (Borko, 2004, p. 13). These arguments are echoed by the National Mathematics Panel Report. “Despite widespread beliefs about the qualities that make teacher education effective, the Panel did not find strong evidence for the impact of any specific form of, or approach to, teacher education on either teachers’ knowledge or students’ learning” (NMP, 2008, p.40). The panel goes on to argue that, “given the vast investment made in teacher education, knowledge about the effectiveness of different approaches is vitally needed. Well-conceived efforts to improve the outcomes of teacher education, to improve measures of those outcomes, and to implement better research strategies should be supported” (NMP, 2008, p. 41). They identify a number of critical questions, including how the duration, structure, quantity, content, pedagogy, and relationship to practice of professional development effects both teachers’ and their students’ learning (NMP, 2008, p.41).

These recommendations highlight two critical issues that need to be addressed by current research. First, they point to the need for large-scale studies. The majority of research into teachers’ learning has been small-scale qualitative studies (see for example, Simon & Schifter, 1991; Jacobson & Lehrer 2000; Wilson, Mattson & Lubienski,1996; see Wilson & Berne, 1999 for this argument more generally). While qualitative research and case studies play an important role highlighting issues with the quality of professional development or identifying features of programs that support teacher development and the dynamics of this learning, they cannot answer questions about how specific features of professional development programs are associated with teachers’ learning, for single programs contain multiple features, and thus it is difficult to tell which of these features are effective. In addition, the findings are often limited to the program or sample of teachers included in the study.

This first issue is directly related to a second. Until recently, researchers have had a limited set of tools at their disposal to study teachers’ knowledge and its growth. Large-scale survey studies have traditionally employed measures of teacher characteristics such as mathematics courses taken, degrees attained, certification, and teaching experience (Begle, 1979). Some have relied on teachers’ own assessment of the professional development or their own learning. In general, researchers have made use of such indirect or proxy measures of teacher knowledge. While informative, these studies cannot
provide guidance on how professional development programs are related to teachers’ actual knowledge and learning. One exception is a study conducted by Hill and Ball (2004) investigating the effects of the California Mathematics Professional Development Institutes on teachers’ mathematics learning. They examined the effects of 15 different institutes on teachers’ learning and found that the institutes had an overall positive effect on teachers’ learning. They also found that both institute length and mathematical focus (e.g., proof/mathematical analysis, communication, representation) were associated with growth in teachers’ mathematical knowledge for teaching. While this study was hampered by the use of data from a pilot version of the LMT instruments and by a generally small sample size, the results suggest that certain program features can have unique effects on teachers’ learning.

By using TKAS to gather data on professional development and teacher knowledge, we seek to contribute to research on professional development by continuing to make widely available measures of mathematical knowledge for teaching for use in both small- and large-scale survey research. We also propose conducting one of the first larger-scale studies to examine how specific features of professional development programs are associated with the development of mathematical knowledge for teaching. We will do this across multiple areas of mathematical knowledge, for teachers of varying backgrounds, and for programs with a variety of design features.

REFERENCES


